

Thermal transfer at crystalline-amorphous interfaces: A Molecular dynamics study

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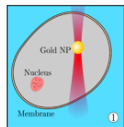


Lyon 1

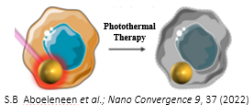


- 1 Introduction
- 2 Interfacial Thermal Conductance Calculations
- 3 Interpretation
- 4 Conclusion

Gold nanoparticles? Bare & Coated



J. Lombard et al.; *Phys. Rev. Res.* (2021)



S.B. Abouleene et al.; *Nano Convergence* 9, 37 (2022)

Figure 1: Biological applications for laser heated gold-nanoparticles

- **Core-Shell nanoparticles** can absorb radiation in the **near-infrared** region where tissues are **transparent**
- How **heat** is transferred between the **core shell nanoparticle** and **water**? What happens at the interface between the **core** and the **shell**?

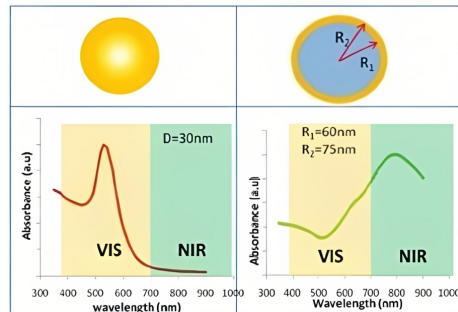
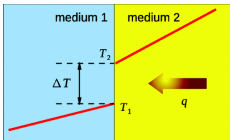
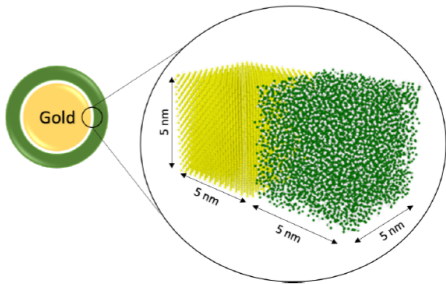


Figure 2: Optical properties of selected gold nanoparticles

Qin and Bischof; *Chemical Society Reviews* 41(3) (2012)

Kapitza Resistance: Thermal Resistance at the Interface



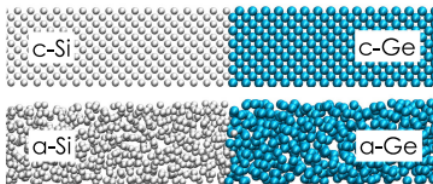
- **First step:** Necessity to calculate the different **Interfacial thermal conductance (ITC)** and **resistance (ITR)**
- There are several methods for performing such calculations; one of the most adapted method is: **Molecular Dynamics**

SM Hatam-Lee et al.; *Nanoscale and Microscale Thermophysical Engineering* (2022)

S. Merabia and K. Termentzidis; *Phys. Rev. B* 86, 094303 (2012)

Phonons in Crystalline and Amorphous Interfaces

- **Crystalline** interfaces exhibit **significantly lower interfacial thermal conductance (ITC)** values of up to 5 times when compared to their **amorphous** counterparts



- Crystalline interfaces → **extended** phonon modes
- Amorphous interfaces → **nonpropagating** phonon modes

- What about **Crystalline - Amorphous** interfaces?

A. France-Lanord et al: J. Phys.: Condens.

Matter 26 355801 (2014)

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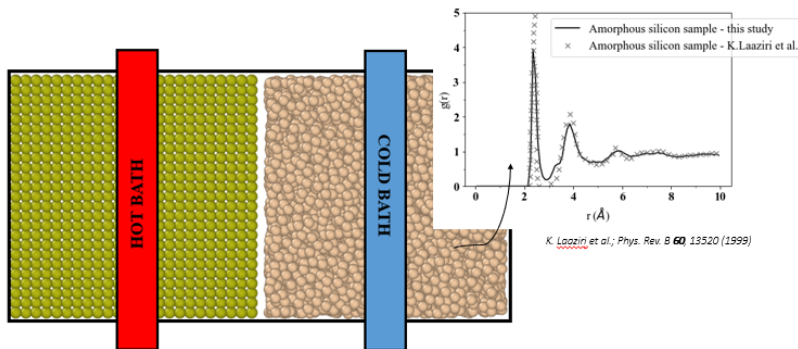
Figure 3: An example of the studied atomic structures of the silicon-germanium interfaces where high ITC is observed in the case of amorphous interfaces

Gordiz and Henry; J. Appl. Phys. 121 (2): 025102 (2017)

Giri et al; J. Appl. Phys. 118, 165303 (2015)

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ITC by Non Equilibrium Molecular Dynamics (NEMD)



- Interfacial thermal conductance (**G**) calculated as:

$$G = \frac{q}{\Delta T \times A}$$

- **q** is the heat flux
- ΔT is the temperature jump at the interface
- **A** is the cross-section

area

ITC by NEMD (Cont'd): Example

- Interfacial thermal conductance calculated as:

$$G = \frac{q}{\Delta T \times A}$$

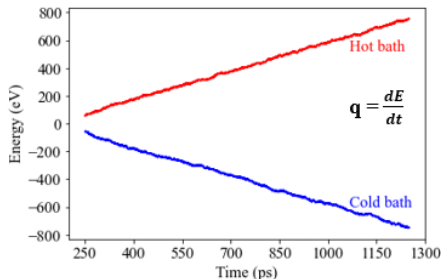


Figure 4: The time-dependent cumulative energy variation of the hot and cold baths

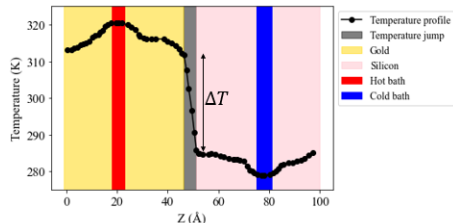


Figure 5: System temperature profile showing the temperature jump at the interface

ITC by NEMD (Cont'd): Results

	ITC (MW/m ² K)	ITR (m ² K/GW)
Gold-Crystalline Silicon	56.61 ± 08	17.85
Gold-Amorphous Silicon	152.17 ± 13	6.57
Gold-Crystalline Silica	102.05 ± 12	9.80
Gold-Amorphous Silica	170.28 ± 14	5.88

- Calculated ITC at the interface of the gold/crystalline-silicon system **agrees** with experimental measurements

R. Cheaito et al.; Phys. Rev. B 91, 035432 (2015)

- The **interfacial thermal conductance** is $\approx$ **3 times** higher for **amorphous** silicon/gold interfaces as compared with **crystalline** silicon/gold interfaces

ITC by NEMD (Cont'd): Temperature and Roughness effect

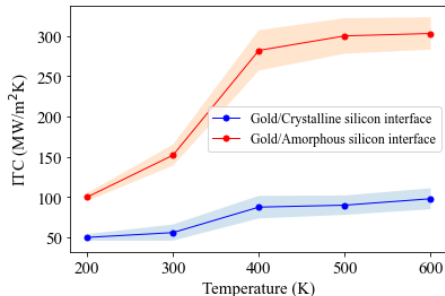


Figure 6: ITC at the gold/crystalline - amorphous silicon interfaces as a function of the system temperature

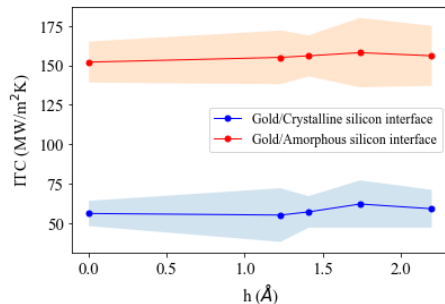


Figure 7: ITC at the gold/crystalline - amorphous silicon interfaces as a function of the height distribution h

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ITC by Diffuse Mismatch Model (DMM)

- Phonon–Phonon ITC is given by the **Landauer's formulation**:

Swartz and Pohl; Rev. Mod. Phys. 61, 605 (1989)

$$G_p = \frac{1}{2} \sum_p \int_0^{\omega_{Au,p}^c} v_{Au,p} \hbar \omega D_{Au,p}(\omega) \frac{\partial f_{eq}(\omega, T)}{\partial T} \int_0^{\pi/2} \alpha_p(\omega, \cos \theta) \cos \theta d(\cos \theta) d\omega$$

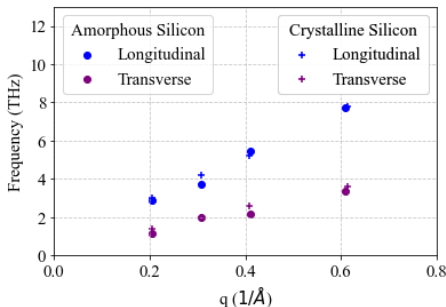


Figure 8: Acoustic dispersion obtained for both silicon structures

ITC (MW/m ² K)	NEMD	DMM
Gold-Crystalline Silicon	56.61	82.7
Gold-Amorphous Silicon	152.17	110

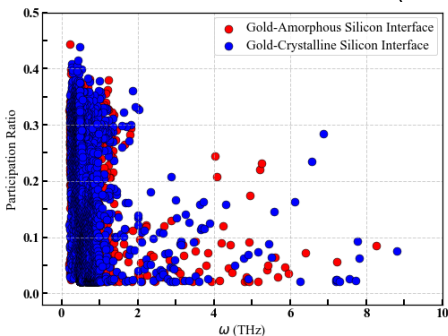
- Huge differences** in between the results of the two approaches
- DMM can't reliably predict results**

Phonon Modal Participation Ratio

- The **phonon modal participation ratio** is calculated as:

Donadio, D et al.; Phys. Rev. Lett. 102, 195901 (2009)

$$P(\mathbf{k}, \nu) = \frac{1}{N_b \sum_1^{N_b} \left(\sum_{\alpha}^3 e_{i,\alpha}^*(\mathbf{k}, \nu) e_{i,\alpha}(\mathbf{k}, \nu) \right)^2}$$



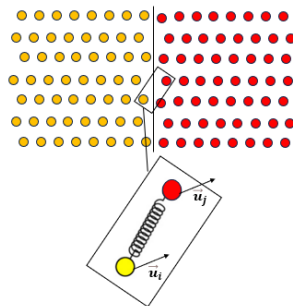
- $P(\mathbf{k}, \nu) \leq 0.5 \rightarrow$ localized phonon mode
- $P(\mathbf{k}, \nu) > 0.5 \rightarrow$ extended phonon mode
- Phonon localization **does not explain** the difference

Figure 9: Phonon modal participation ratio at both interfaces

How to Explain this Threefold Increase?

- **Calculated average** spring stiffness acting on a gold atom is about **30% greater** at the crystalline-amorphous silicon interfaces
- **Higher cross-correlation coefficient** between **atomic vibrational displacements** at the crystalline-amorphous silicon interfaces which directly influence ITC

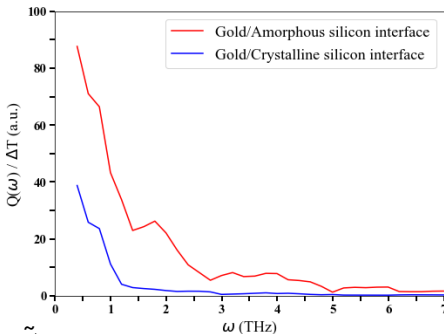
X. Li et al.; Nanoscale, 15, 8603-8610 (2023)



- **How can we combine these two quantities?**

Frequency dependent Spring stiffness-atomic displacement Spectrum

- $Q(\omega)$ encodes the combined information on the **Spring stiffness** and the **atomic displacements cross-correlation**



$$Q(\omega) = \frac{-i\omega}{2} \left[\sum_{i \in Au} \sum_{j \in Si} \vec{K}_{ij} \langle \tilde{\vec{\Delta}}_{ij}(\omega) \cdot \tilde{\vec{\Delta}}_{ij}^*(\omega) \rangle \right]$$

$$\text{Where: } \tilde{\vec{\Delta}}_{ij}(\omega) = \tilde{\vec{u}}_i(\omega) - \tilde{\vec{u}}_j(\omega); \text{ with: } \tilde{\vec{u}}_i(\omega) = \int_0^{t_{\max}} \vec{u}_i(\tau) e^{i\omega\tau} d\tau$$

- **Low frequencies are involved!**

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Conclusion

- Characterize the **interfacial thermal resistance** at the different interfaces
- Report a **threefold increase** of interfacial thermal conductance for gold-amorphous interfaces
- Interpret this result by **enhanced bonding** and **atomic displacements cross correlations of low frequency phonon modes** at the interfaces

Thank You!



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Lyon 1

